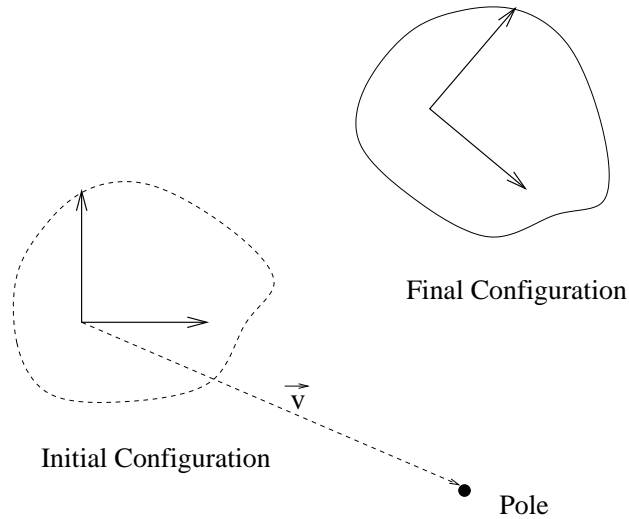


ME 115(a): Homework #1

(Due Friday January 25, 2008)

Problem 1: (10 points) Every planar rigid body displacement is *equivalent* to a rotation about a unique point in the plane, known as the pole (see Figure).



Let A be a fixed reference frame. A rigid body, L , which has local frame B attached to it, is located relative to reference frame A by $D_1 = (\vec{d}_{01}, R_{01},)$. Body L moves to position C , where the displacement to location C , as measured by an observer in frame B , is given by $D_2 = (\vec{d}_{12}, R_{12})$. Where is the *pole* of the body displacement from position B to position C , as a function of R_{01} , R_{12} , \vec{d}_{01} , and \vec{d}_{12} ?

- As measured in Frame A
- As measured in Frame B
- As measured in Frame C

Problem 2: (5 points) In the above problem, suppose $D_1 = (x, y, \theta) = (1.0, 2.0, 30.0^\circ)$ and $D_2 = (x, y, \theta) = (2.0, 2.0, 45^\circ)$. Where is the pole of the displacement from B to C in this case?

Problem 3: (15 points) Using the set up of Problem 1, pick a coordinate system whose origin is located at the pole of the displacement, and show that in this coordinate system, the displacement of the body from B to C is a pure rotation.

Problem 4: (15 points) A *planar reflection* is an operation wherein one “reflects” all of the particles in a body across a line. Show (intuitively) that reflections “preserve length.” That

is, reflections do not alter the distance relationship between particles in a rigid body. Can any planar displacement be equivalently performed by a reflection?

Problem 5: (10 points) In class we used the particle nature of rigid bodies to “prove” that a planar rigid body has three degrees of freedom. Use the same idea to “prove” that a body undergoing spherical motion has three degrees of freedom.