

**ME 115(b): Homework #3**  
(Due Wednesday, April 26, 2006)

**Problem 1:** Problem 21(a,b,c,e), Chapter 3 of MLS.

**Problem 2:** (Special Configurations of a linkage). Consider the linkage shown Figure 1. This problem considers the stationary configurations of this mechanism.

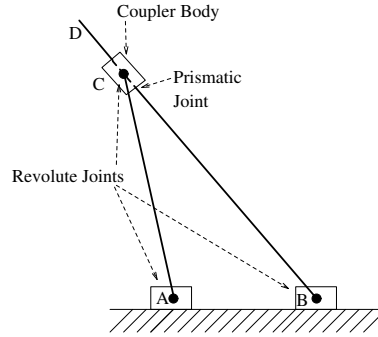


Figure 1: Mechanism

In this mechanism, let  $|\overline{AB}| = 1$ . The dimension  $|\overline{AC}| = l_1$  is variable, and will be determined below.

- (a) derive the twist coordinates for the joint axis screws.
- (b) It was shown in class that the special (or stationary) configurations for the  $j^{th}$  joint occur when the determinant of the cofactor of the  $jj$  element of the grammian matrix:

$$\begin{bmatrix} \xi_1 \cdot \xi_1 & \xi_1 \cdot \xi_2 & \xi_1 \cdot \xi_3 & \xi_1 \cdot \xi_4 \\ \xi_2 \cdot \xi_1 & \xi_2 \cdot \xi_2 & \xi_2 \cdot \xi_3 & \xi_2 \cdot \xi_4 \\ \xi_3 \cdot \xi_1 & \xi_3 \cdot \xi_2 & \xi_3 \cdot \xi_3 & \xi_3 \cdot \xi_4 \\ \xi_4 \cdot \xi_1 & \xi_4 \cdot \xi_2 & \xi_4 \cdot \xi_3 & \xi_4 \cdot \xi_4 \end{bmatrix}$$

becomes zero (where  $\xi_j$  denotes the twist for joint axis  $j$ ).

Develop an expression for the stationary configurations of joint 1. What are the necessary conditions (in terms of link lengths, etc.) for joint 1 to have a stationary configuration?

- (c) Do any other joints have stationary configurations?

**Problem 3:** Problem 1(a) Chapter 3 of MLS.

**Problem 4:** Problem 2(a) Chapter 3 of MLS.